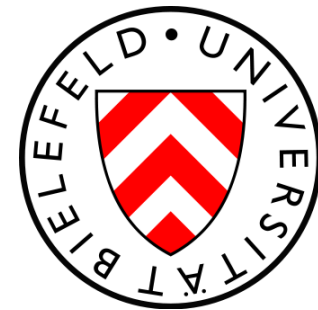


The known, the novel, the unexpected: Particle Physics in the LHC era



Prof. Dr.
York Schröder



Bielefeld Physics Colloquium, 17 May 2010

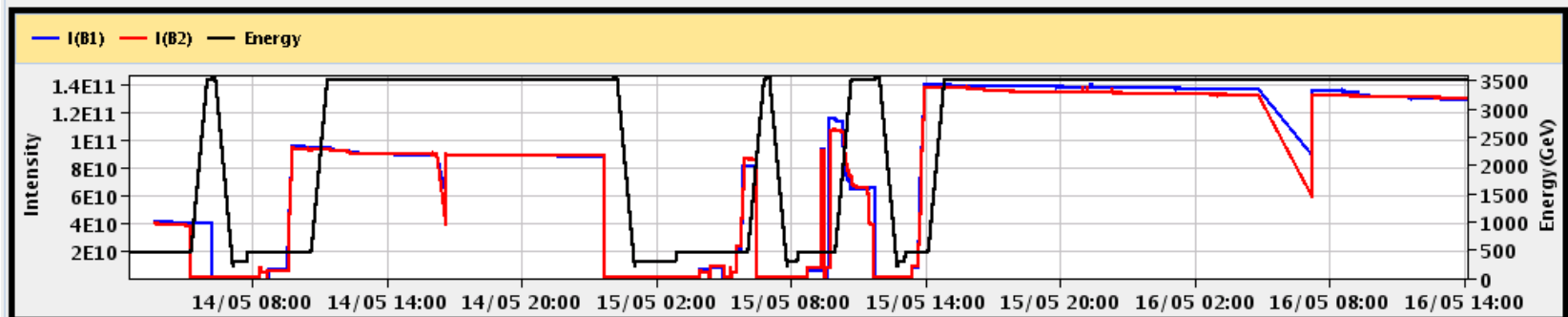
LHC: Status 16-05-2010

16-May-2010 14:07:08 Fill #: 1104 Energy: 3500.3 GeV I(B1): 1.28e+11 I(B2): 1.30e+11

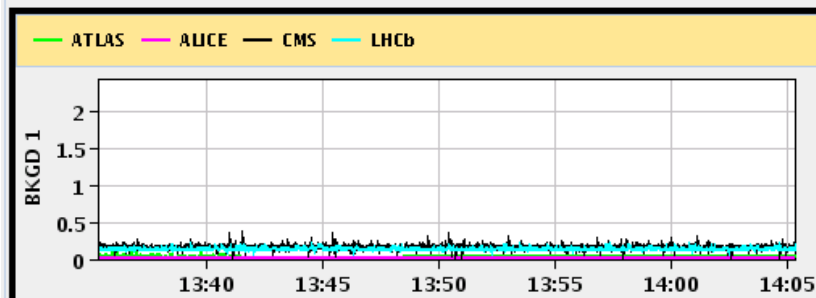
	ATLAS	ALICE	CMS	LHCb
Experiment Status	STANDBY	CALIBRATION	STAND...	STAND...
Instantaneous Luminosity	5.114e-02	0.000e+00	5.072e-02	3.755e-02
BRAN Count Rate	6.900e+02	2.960e+02	1.110e+03	8.450e+02
BKGD 1	0.042	0.006	0.140	0.122
BKGD 2	0.000	0.000	19.268	2.781
BKGD 3	0.000	0.002	0.003	0.034

LHCf	MOVING	Count(Hz): 0.000	LHCb VELO Position	m	Gap: -0.0 mm	TOTEM:	CALIBRATION
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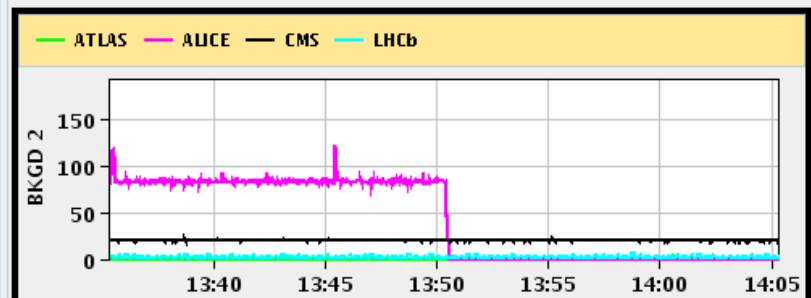
Performance over the last 12 Hrs



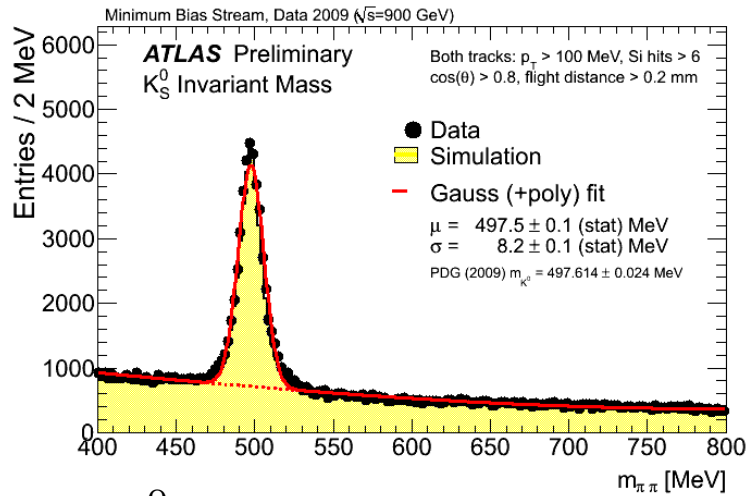
Background 1



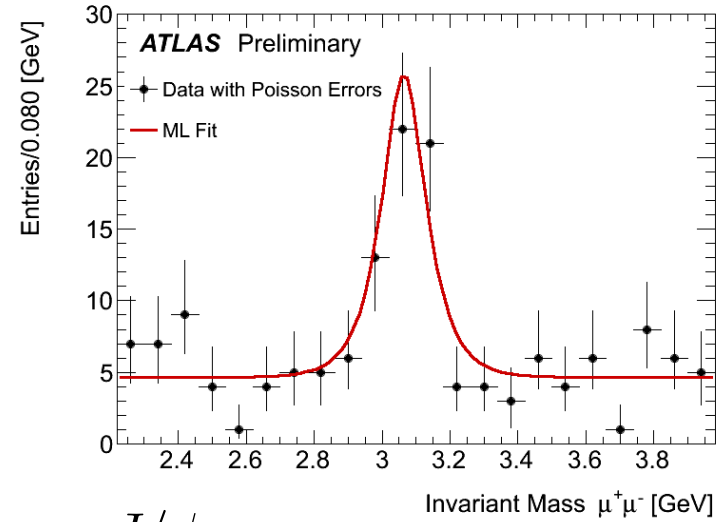
Background 2



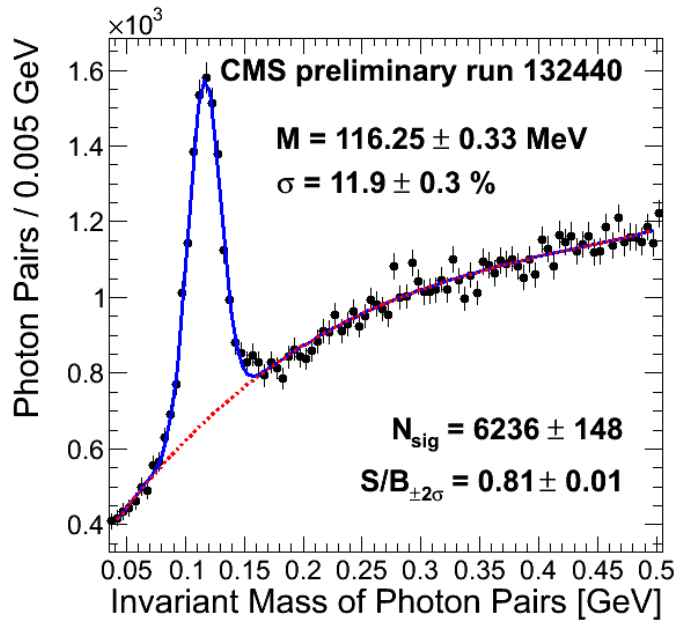
SM rediscovered at LHC: heavy flavor and W



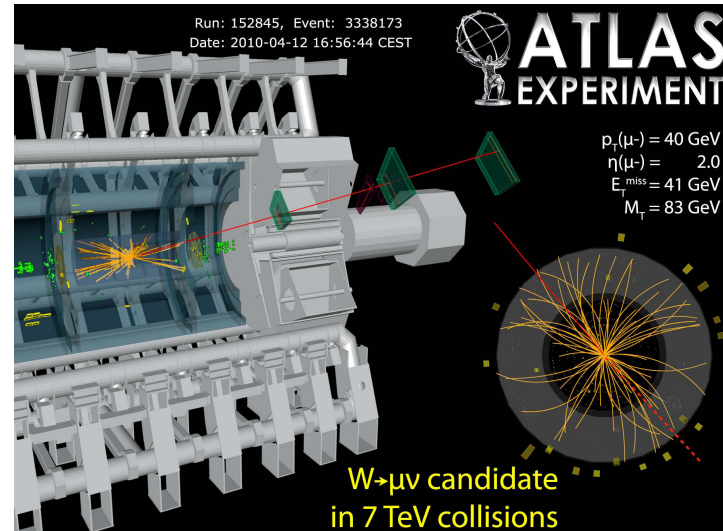
$$K_S^0 \rightarrow \pi \pi$$



$$J/\psi \rightarrow \mu \mu$$

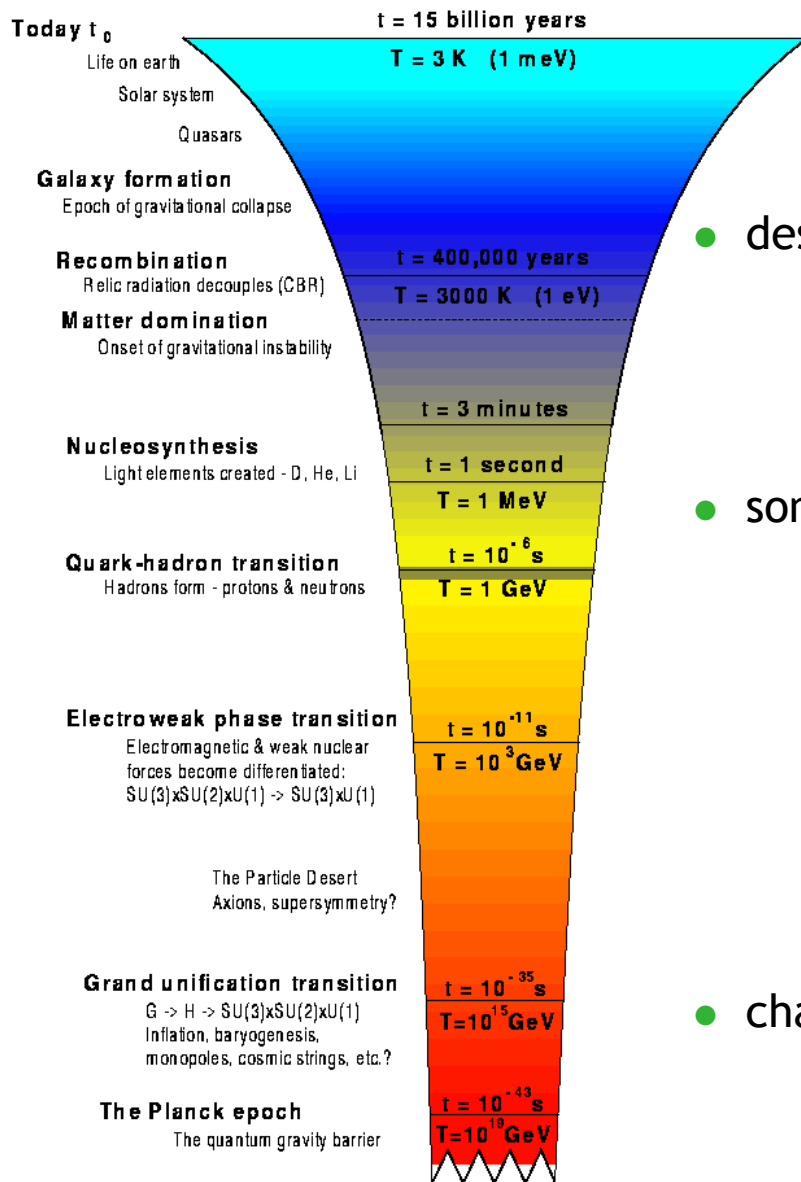


$$\pi^0 \rightarrow \gamma \gamma$$



$$W \rightarrow \mu \nu \text{ candidate}$$

Motivation: think BIG!



ask fundamental questions about physics
 → deepest laws of nature?
 → structure of space and time?

- describe physics in universal framework
 - ▷ QFT (= QM + Rel) + SM + (class.) Grav [YS, Colloq 2007]
 - ▷ \emptyset universe - particles - Planck length
 10^{28} cm - 10^{-17} cm - 10^{-33} cm
- some of the big open questions
 - ▷ nature of electroweak symmetry breaking?
 - ▷ nature of Quark-Gluon plasma?
 - ▷ origin of matter/antimatter asymmetry?
 - ▷ Quark or Lepton substructure?
 - ▷ supersymmetry? dark matter?
 - ▷ embedding of SM in GUT?
 - ▷ QM \cap Gravity; strings? extra dimensions?
- challenging questions; concern smallest distance scales
 - ▷ use powerful microscope to explore
 - ▷ Uncertainty (Heisenberg) + Relativity \Rightarrow high E, m

Standard Model (SM)

Elementary particles \equiv ultimate building blocks

Three Generations
of Matter (Fermions)

	I	II	III	
mass \rightarrow	2.4 MeV	1.27 GeV	171.2 GeV	0
charge \rightarrow	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
spin \rightarrow	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
name \rightarrow	u up	c charm	t top	γ photon
	4.8 MeV	104 MeV	4.2 GeV	0
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	d down	s strange	b bottom	g gluon
	<2.2 eV	<0.17 MeV	<15.5 MeV	91.2 GeV
	0	0	0	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	Z⁰ weak force
	0.511 MeV	105.7 MeV	1.777 GeV	80.4 GeV
	-1	-1	-1	± 1
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	e electron	μ muon	τ tau	W[±] weak force

Bosons (Forces)

● known:

● predicted / anticipated:

- ▷ Higgs-Boson(s)
- ▷ SUSY-particles, dark matter [5× ordinary baryonic matter!]
- ▷ axions?, ...

Quantum Field Theory (QFT)

Quantum Field Theory \equiv nature of interactions

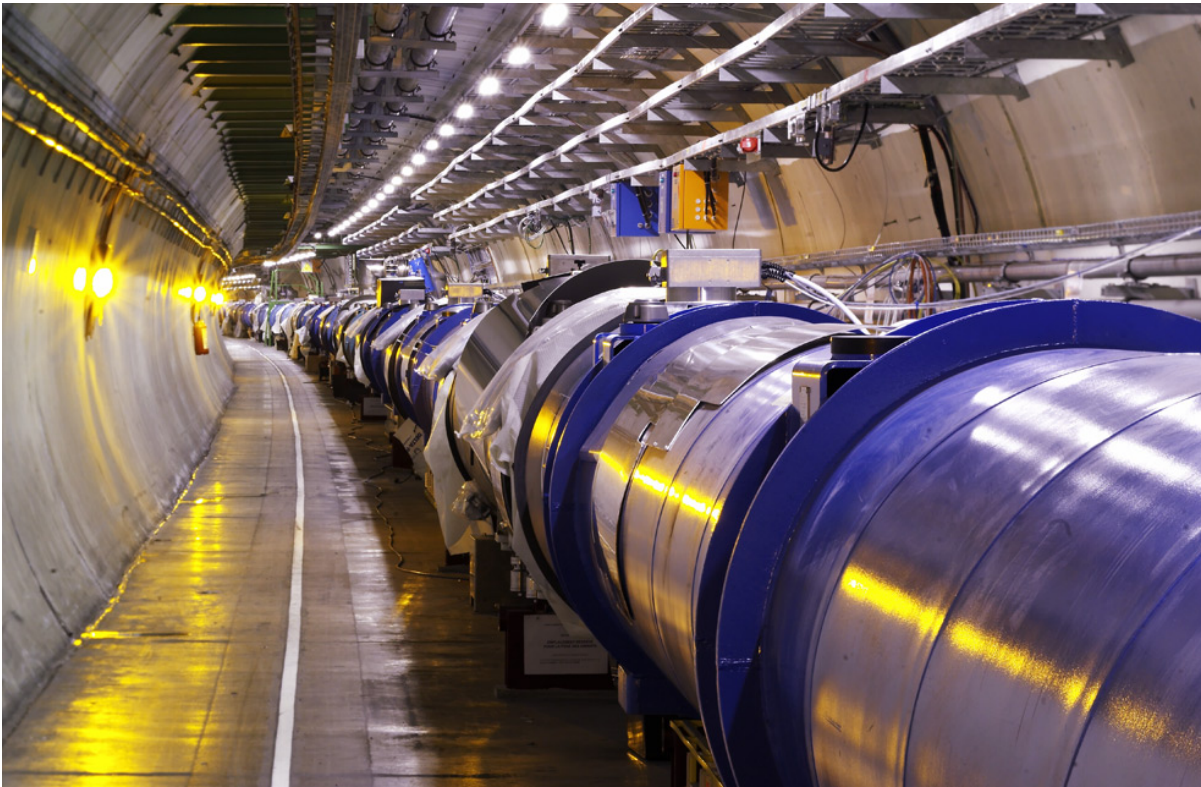
- known: $\mathcal{L}_{SM} = \mathcal{L}_{QCD} + \mathcal{L}_{EW}$
- predicted / anticipated:
 - ▷ healthy local gauge theory
 $SU(3)_C \times SU(2)_L \times U(1)_Y$ (g-WZ- γ)
 - ▷ extra dimensions?
 - ▷ monopoles? strings?
 - ▷ grand unification (GUT)
 - ▷ ...

- some important experiments (colliders since 70s; here \geq 90s)

name	place	type	E_{cm} [GeV]	time	highlight
LEP	CERN, Geneva	e+e	209	1989-2000	Z-, W-Boson
HERA	DESY, Hamburg	e+p	318	1992-2007	Gluon
Tevatron	Fermilab, Chicago	p+p	2000	1983-2010(?)	Top-Quark
LHC	CERN, Geneva	p+p	14000	2009 -	Higgs-Boson?, ...
ILC	?	e+e	500-1000	20?? -	...

Particle Colliders: LHC data sheet

- 2×2800 bunches à 12 billion protons; collisions every 25 ns
- max. p+p energy in center-of-mass-(=lab)-system: $\sqrt{s} = 14 \text{ TeV}$ [cf. Tevatron: 1.96 TeV]



- ca 3 billion Euro
- 27 km tunnel
- 1200 dipole-magnets
- B-field up to 8.6 Tesla
- 1.9°K; 90t liquid He
- these parameters
 - $E_{max} = 7 \text{ TeV}$
 - $v = 0.999999991 c$

- central quantity: **Luminosity**; designed for $L = \frac{10^{33} \dots 10^{34}}{cm^2 s}$ [or $\frac{1 \dots 10}{nb s}$]
- for a specific process: Event rate = **Luminosity** \times Cross section

Operational challenges

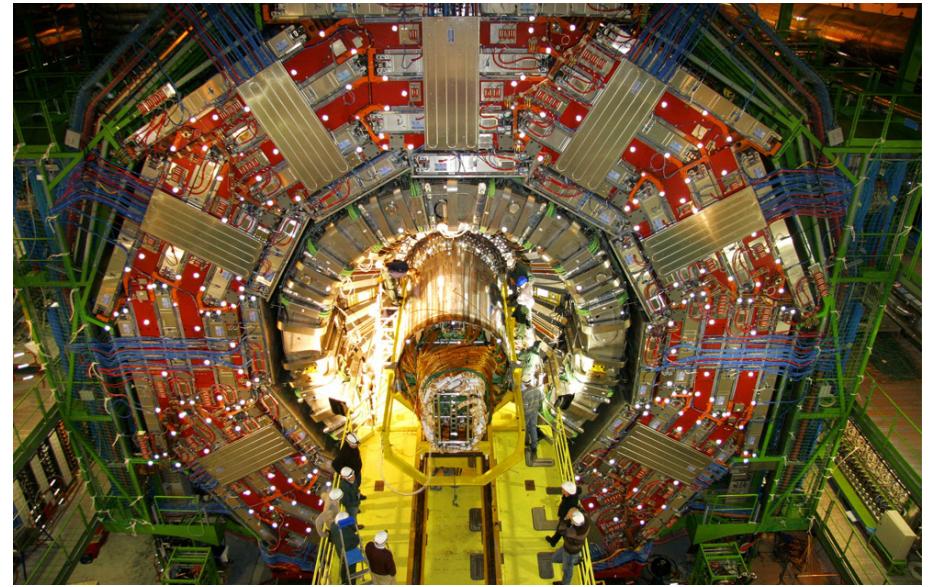
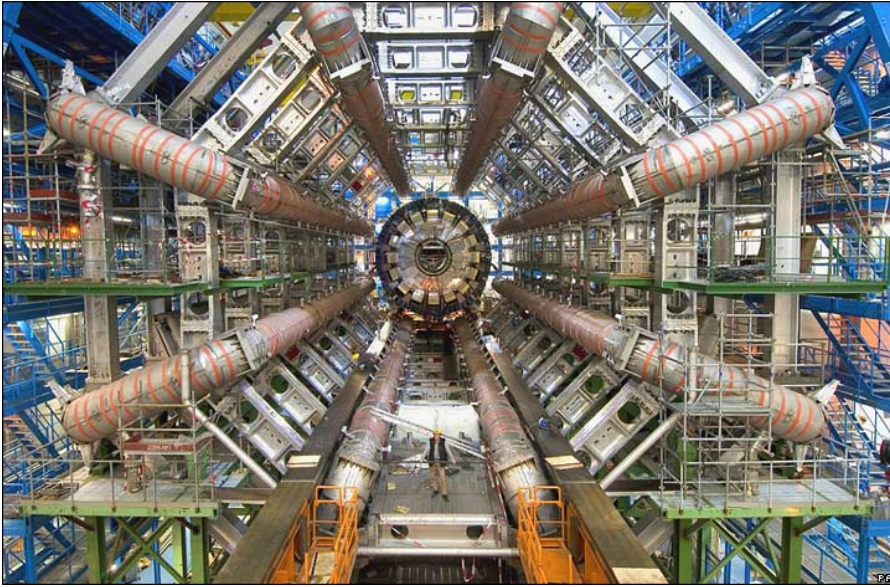
- have built the LHC - now learn how to **operate powerful machine**
- energy stored in magnets(beam): $10(0.7)$ GJ $\approx 2.4(0.2)$ tons of TNT
 - ▷ beam dump!
 - ▷ compare: 1 fill $\approx 10^{-9}$ grams of Hydrogen
 - ▷ loss of 10^{-7} part of beam \rightarrow supercond. magnet quench



- 2008 run
 - ▷ 10 Sep: Protons circulating
 - ▷ 19 Sep: quench in dipole magnets!!
 - ▷ loss of 6t He; 1 year repair
- 2009 run
 - ▷ 23 Nov: **collisions** at 450 GeV (1 bunch)
 - ▷ 30 Nov: 1.18 TeV per beam (beat 0.98)

- 2010/2011 run
 - ▷ Mar: ramp up Energy to 3.5 TeV
 - ▷ since 30 Mar: 3.5 TeV + 3.5 TeV **collisions** (4 bunches)
 - ▷ operate continuously to end of 2011; or until 1 fb^{-1} seen per experiment
 - ▷ current status: each expt has recorded 1 nb^{-1}

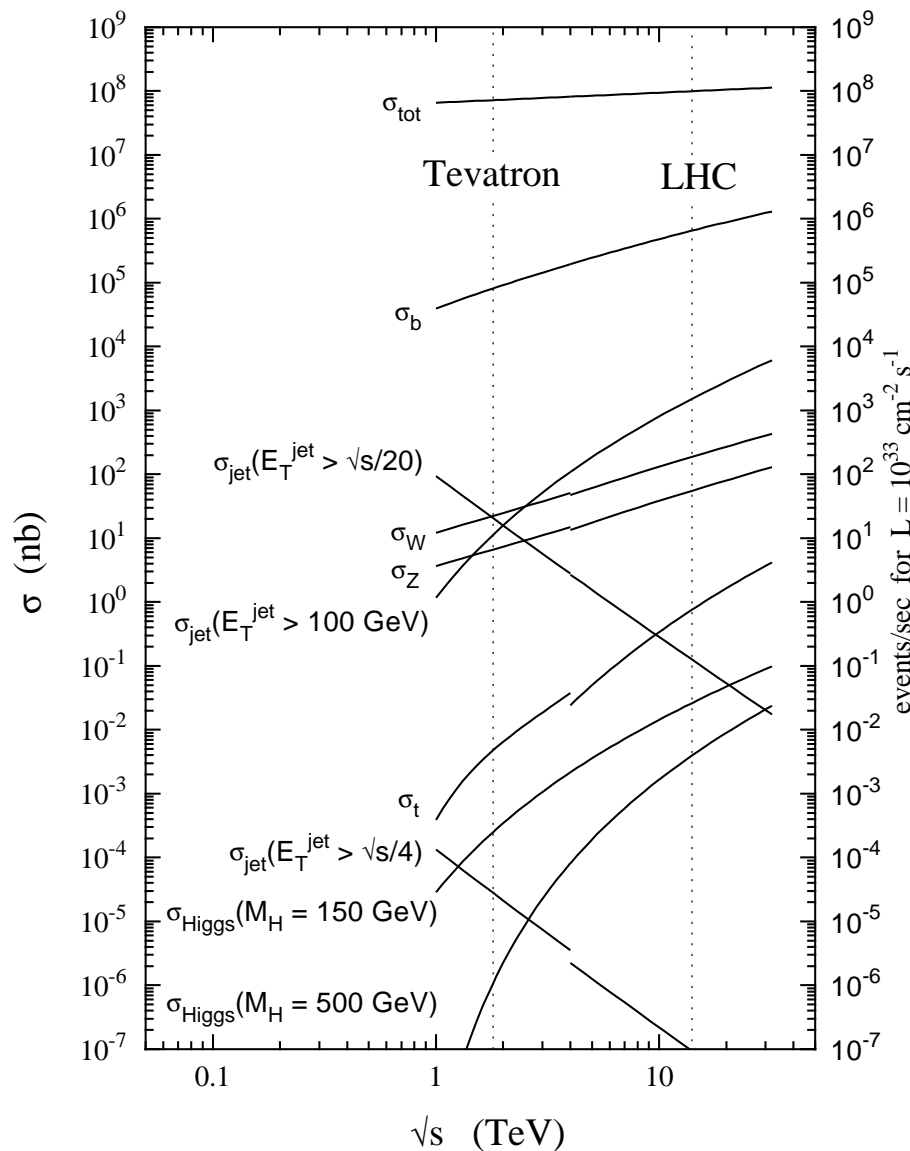
Main LHC - Detectors



- ATLAS - A Toroidal LHC Apparatus
 - 45×22×22 m, 7000 tons
 - 1870 physicists ∈ 150 institutes
 - data rate 100000 CD's/sec → save 27 CD's/min
 - 22 simultaneous pp-collisions per "event" (on average)
 - often signal/background < 10^{-10} !!
- CMS - Compact Muon Solenoid
 - 21×16×16 m, 12500 tons
 - 2300 physicists ∈ 159 institutes

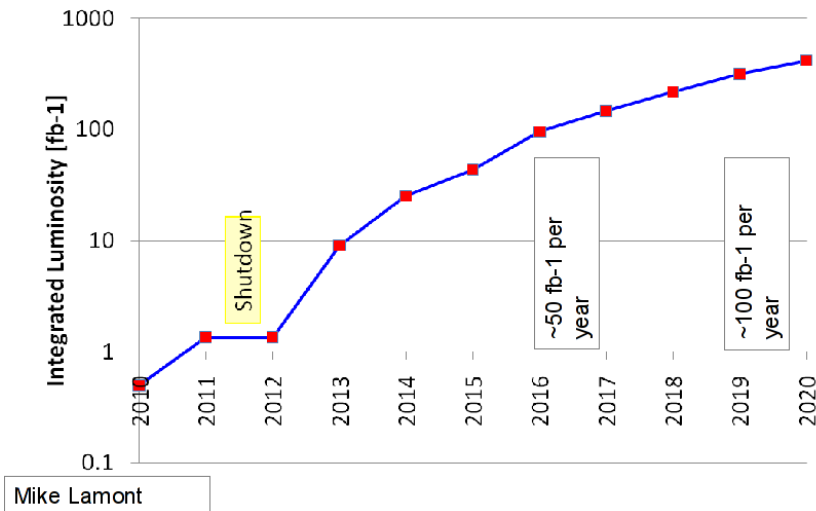
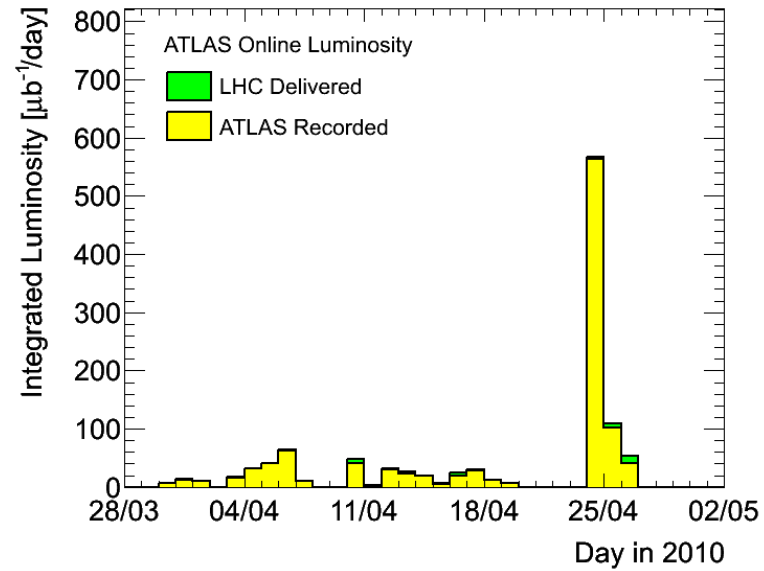
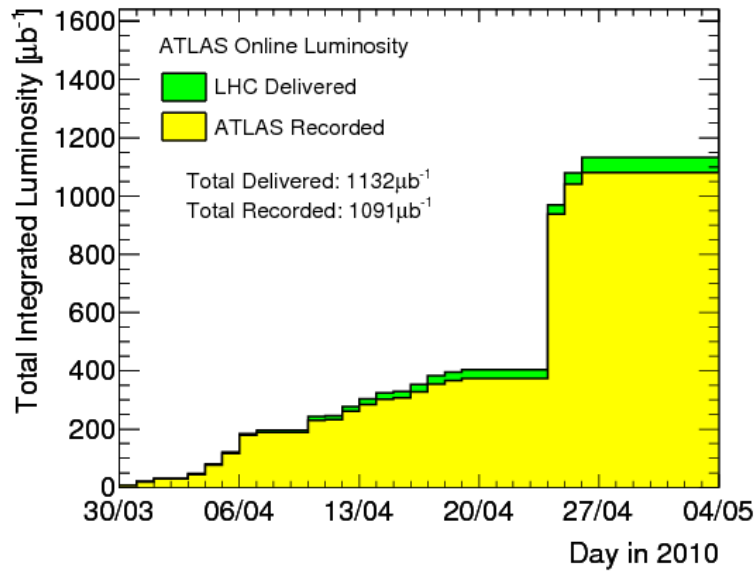
LHC - typical event rates

proton - (anti)proton cross sections



- low LHC (**design-**) Luminosity
- 10^8 pp-collisions per second
- signal vs background!
- in each second produce:
 - ▷ 200 W-Bosons
 - ▷ 50 Z-Bosons
 - ▷ 1 $t\bar{t}$ -pair
- in each minute produce:
 - ▷ 1 light Higgs
- currently \approx (these #s)/ 10^5

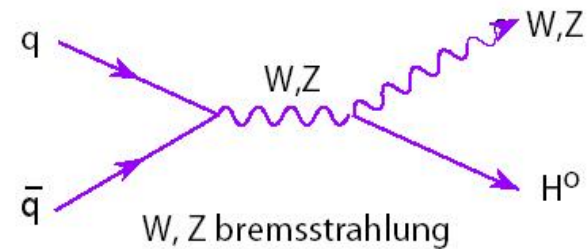
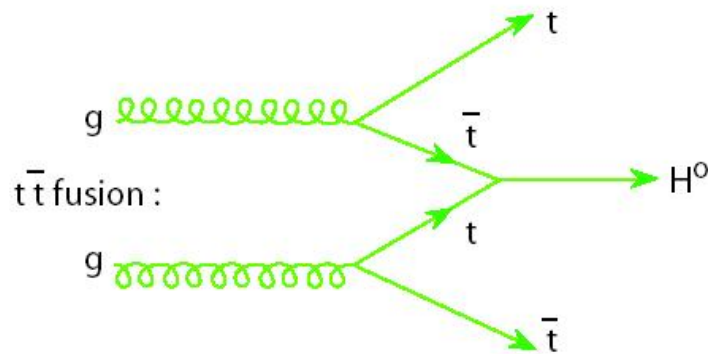
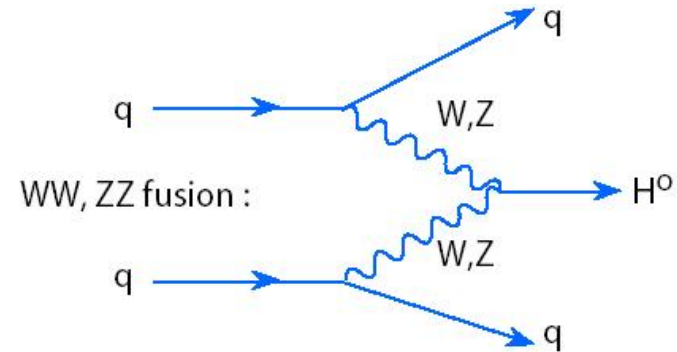
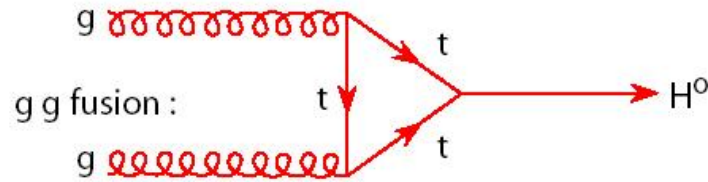
LHC - Luminosity



- ▷ ATLAS/CMS have recorded $\sim 1 \text{ nb}^{-1}$ each (see above)
- ▷ LHC running at $E/2$ and $L/10^6$
- ▷ cf. Tevatron record: total 8 fb^{-1}
 $2 \text{ fb}^{-1}/\text{yr}$; $250 \text{ pb}^{-1}/\text{mo}$; $73 \text{ pb}^{-1}/\text{wk}$
- ▷ much more to come (see left)

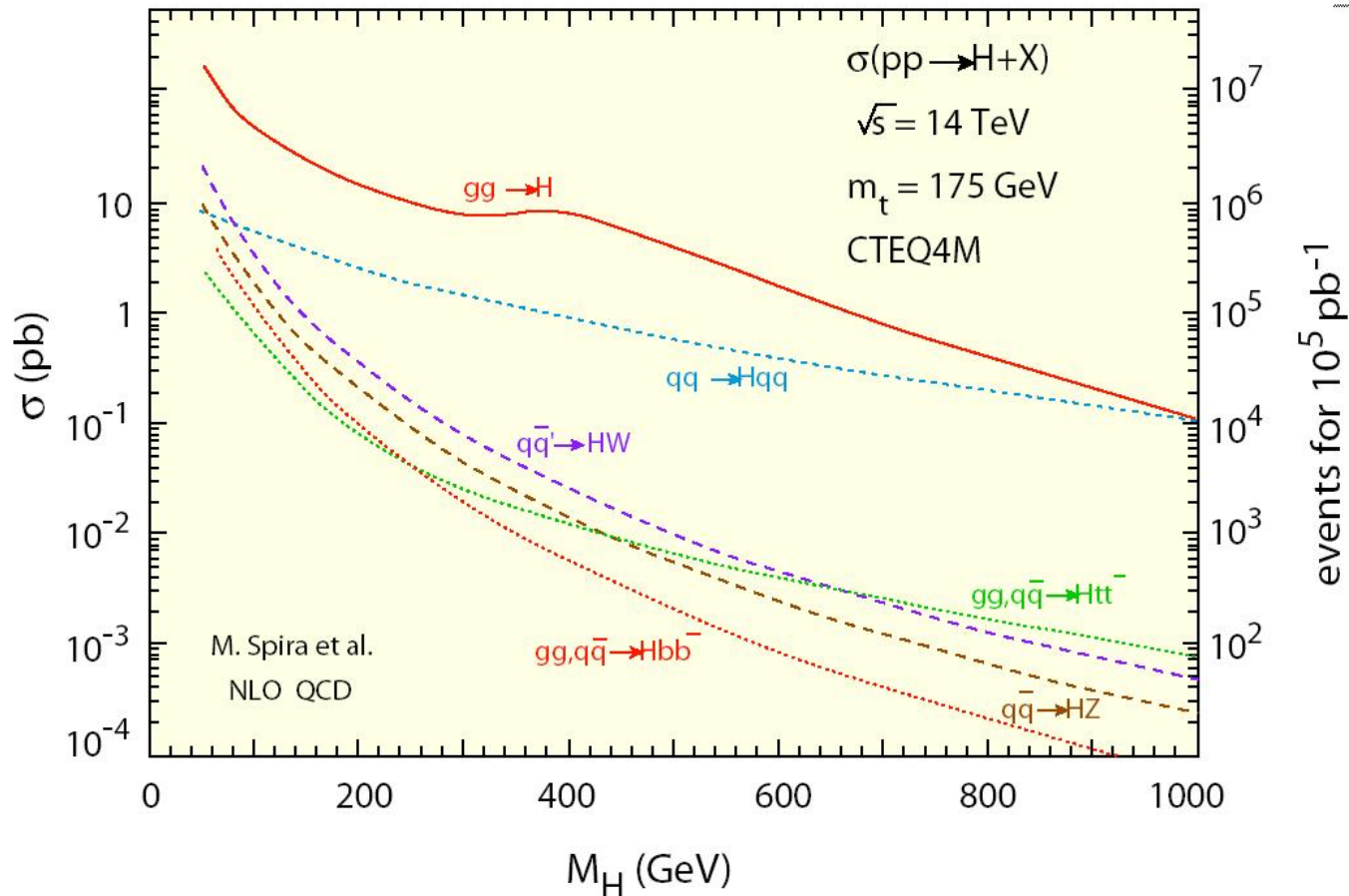
How are Higgs-Bosons produced?

- Protons consist of Quarks+Gluons (LHC as Gluon-collider)



- graphical representation: Feynman diagrams
- sometimes, loops are dominant! (cf. next pg)

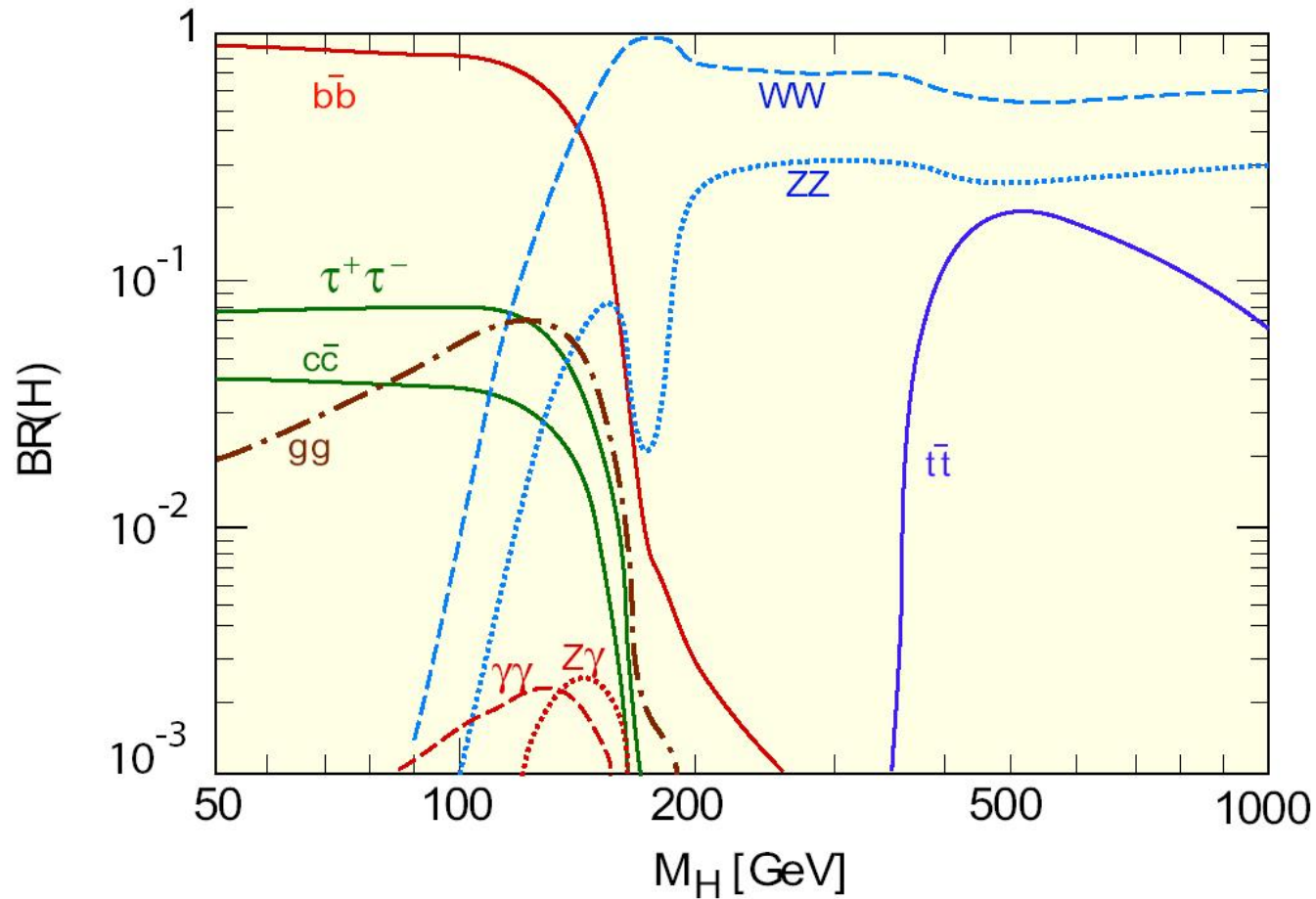
How many Higgs-Bosons are produced?



- CTEQ4M are “structure functions”: distribution of Quarks+Glucos in Proton
- events per year (eff. 10^7 sec) at LHC with high Luminosity ($1 \text{ pb} = 10^{-36} \text{ cm}^2$)
- **most important production process: Gluon fusion**

Higgs decay rates

- branching ratios show strong dependence on Higgs-mass



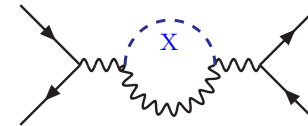
- most important decay channel: $b\bar{b}$ / WW
- number of observed events is $N_{x,obs} = L \cdot \sigma_x \cdot BR \cdot \Delta t \cdot \varepsilon$

Sensitivity on yet-unknown physics

- explore a new energy range
 - ▷ search for “expected” signals of new physics (e.g. Higgs) [known unknowns]
 - ▷ keep an open mind for unexpected new physics [unknown unknowns]

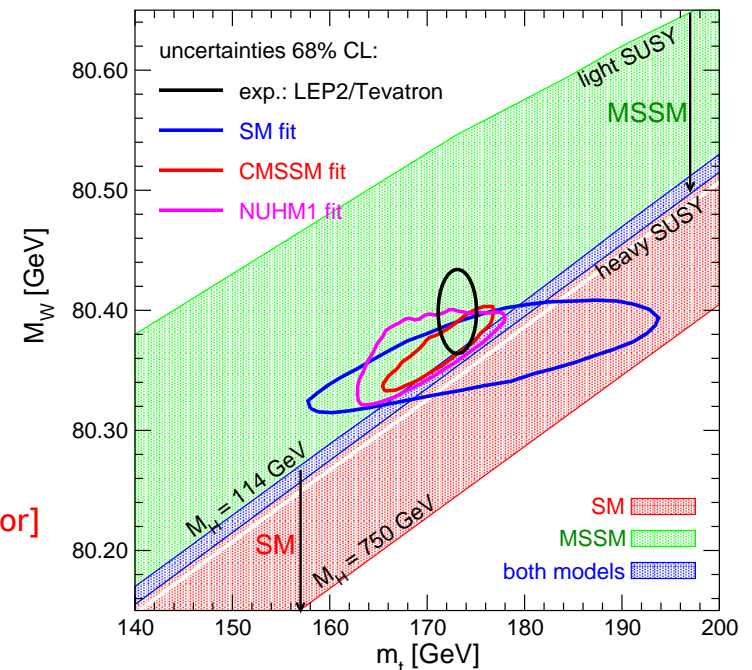
- perform precise SM tests

- ▷ high sensitivity on BSM physics in precision measurements: **quantum corrections!**
- ▷ use SM measurements to “gauge” detectors
- ▷ understand SM at $\sqrt{s} = 14$ GeV; check Monte-Carlo generators etc.

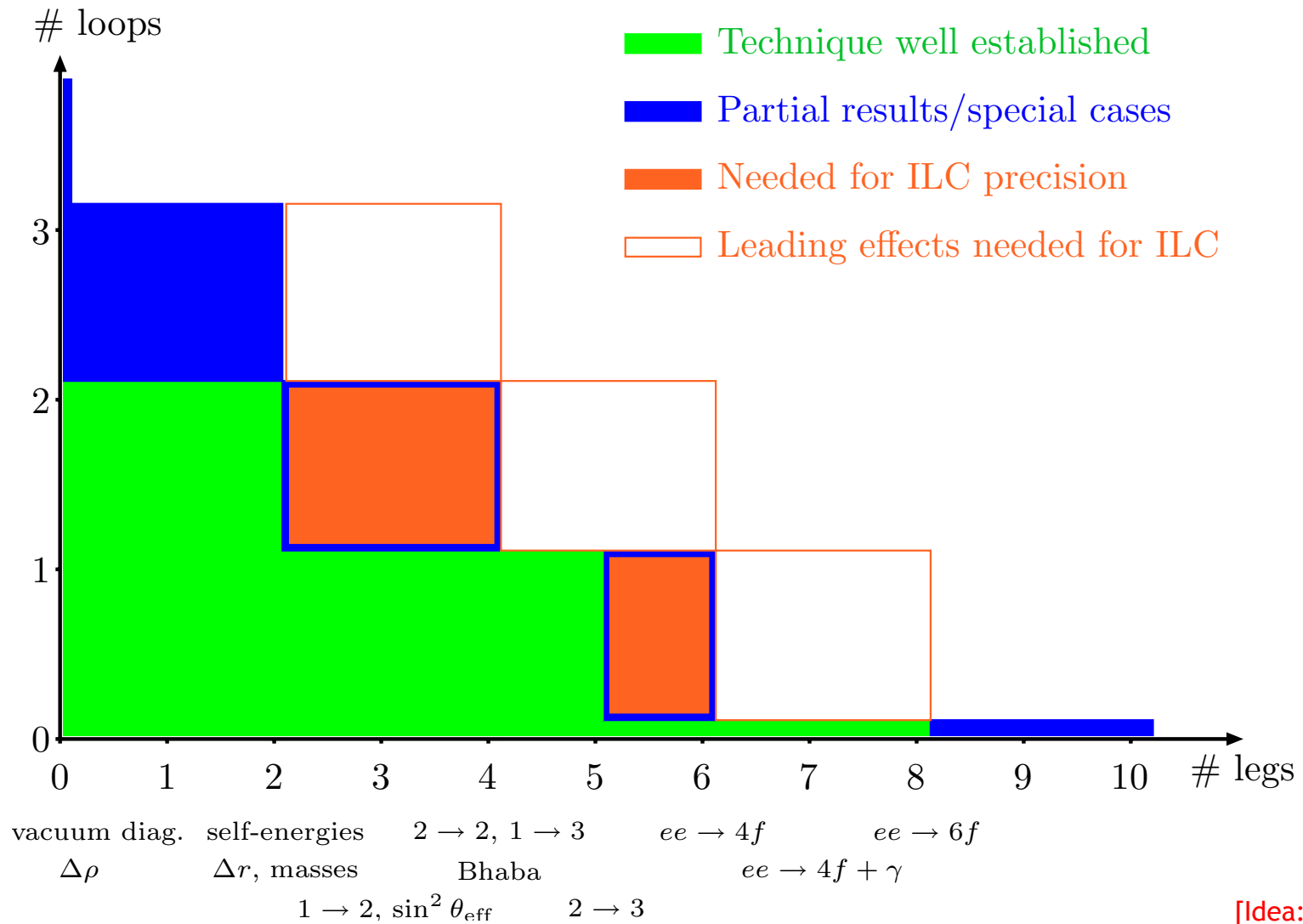


- experimental limits ↔ theoretical precision

- ▷ e.g. SUSY search
 \tilde{q}, \tilde{g} produced via strong int cascade decay → LSP
- ▷ missing energy? e.g. Jets + E_T^{miss}
- ▷ establish SUSY mass scale
- ▷ determine model parameters (hard! ILC..)
- ▷ **cave:** only two models here [O.Buchmüller et al.]
 many alternatives [little Higgs, Xtra dim, ext technicolor]
 all predict new sub-TeV particles!



Loops+Legs - sports



→ in the following: three examples; mostly from ‘‘upper left’’

(1) Gauge boson masses at high precision

- experiment: ILC @ Z-resonance ($M_W = 80404 \text{ MeV}$)
 - ▷ → measurement with $\delta M_W^{exp} = 6 \text{ MeV}$ possible
 - ▷ compare with current $\delta M_W^{exp} = 30 \text{ MeV}$

- theory: SM contains prediction for $M_W(M_Z, G_F, \alpha, \delta\rho)$

where $\delta\rho =$ elektroweak rho parameter [Veltman 1977]

$=$ ratio of neutral to charged current

$$= \frac{\Pi_T^{ZZ}(0)}{M_Z^2} - \frac{\Pi_T^{WW}(0)}{M_W^2}$$

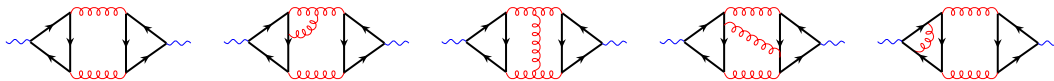
- computation: $\delta\rho = 1 + \#\alpha_s + \#\alpha_s^2 + \#\alpha_s^3 + \dots$

where $\alpha_s \approx 1/10$

▷ $\alpha_s^1 \Rightarrow \delta M_W = -60 \text{ MeV}$ [Djouadi 1988]

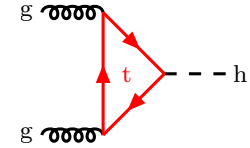
▷ $\alpha_s^2 \Rightarrow \delta M_W = -10 \text{ MeV}$ [Fleischer, Tarasov 1994]

▷ $\alpha_s^3 \Rightarrow \delta M_W = +0.2 \text{ MeV}$ [YS, Steinhauser 2005]



(2) Heavy quark decoupling relations

- primary production channel for Higgs-Bosons at LHC: Gluon fusion ($g + g \rightarrow H$)
- decay channel analogous ($H \rightarrow g + g$)
- theory: processes are loop-induced (see above)



→ higher perturbative orders extremely important!

▷ e.g. $\Gamma(H \rightarrow gg) = \frac{G_F M_H^2}{36\pi\sqrt{2}} \left(\frac{\alpha_s}{\pi}\right)^2 \cdot K$

▷ where $K \sim 1 + \#\alpha_s + \#\alpha_s^2 + \#\alpha_s^3 + \dots$

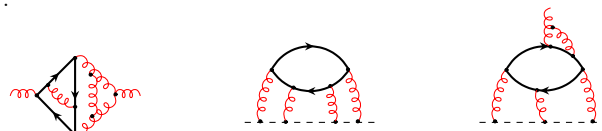
resp $K \sim 1 + 0.656 + 0.204 + 0.019 + \dots$ [Baikov,Chetyrkin 2006]

- need to know coupling α_s with extreme precision
- experiment: determine α_s at “low” energy
e.g. in Tau decays ($M_\tau = 1.777$ GeV)
→ $\alpha_s(M_\tau) = 0.345 \pm 0.004_{exp} \pm 0.008_{th}$
- strategy: evolve α_s to higher energies
e.g. to $\alpha_s(M_Z) = 0.1216 \pm 0.0004_{exp} \pm 0.0010_{th} \pm 0.0004_{evol}$ ($M_Z = 91.2$ GeV)
→ running coupling; RG-equations; beta function $\beta(N_f = \#$ of light Quarks)
→ cf. mass(u, d, s, c, b, t) \approx (0.002, 0.004, 0.095, 1.25, 4.2, 174) GeV

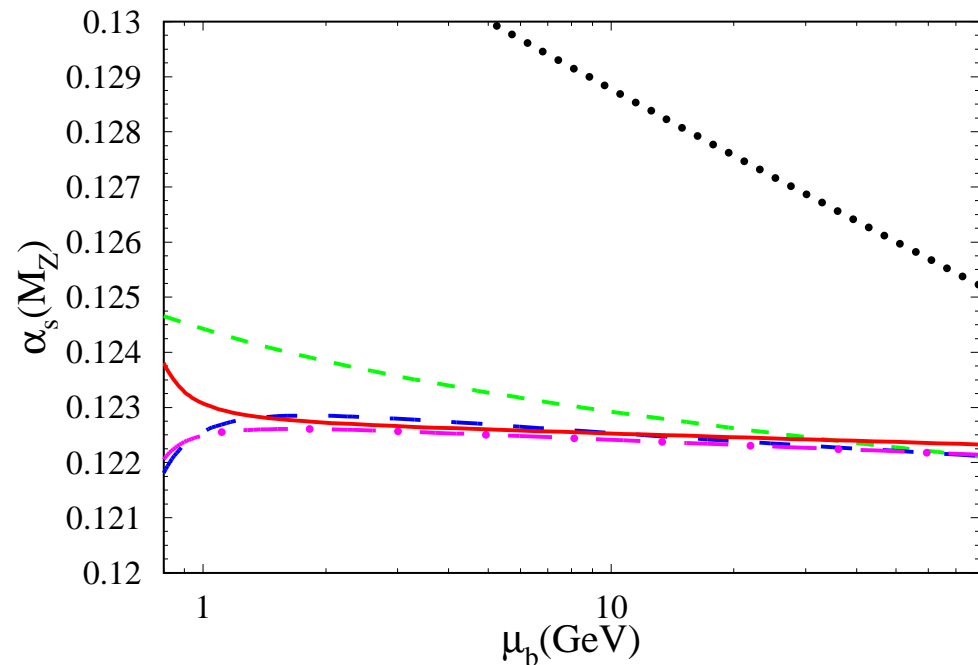
(2) Heavy quark decoupling relations

- crossing the b -Quark threshold
 → main idea: integrate out effects of heavy Quarks

- strategy: $\alpha_s^{(4)}(M_\tau) \xrightarrow{\text{run } N_f=4} \alpha_s^{(4)}(\mu) \xrightarrow{\text{dec } 4 \leftrightarrow 5} \alpha_s^{(4)}(\mu) \xrightarrow{\text{run } N_f=5} \alpha_s^{(5)}(M_Z)$

- computation: 

- μ scale dependence?
 - ▷ unphysical
 - ▷ has to vanish!
 - ▷ depends on decoupling precision
 - ▷ result: 4-loop flat [YS,Steinhauser 2006]



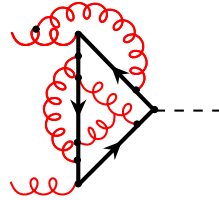
(2) Heavy quark decoupling relations

- \Rightarrow precise evolution of “running” coupling $\alpha_s(E)$
- another amusing application of decoupling relations:

building block for (5-loop)

$$\Gamma(H \rightarrow gg)$$

$$\sigma(gg \rightarrow H)$$



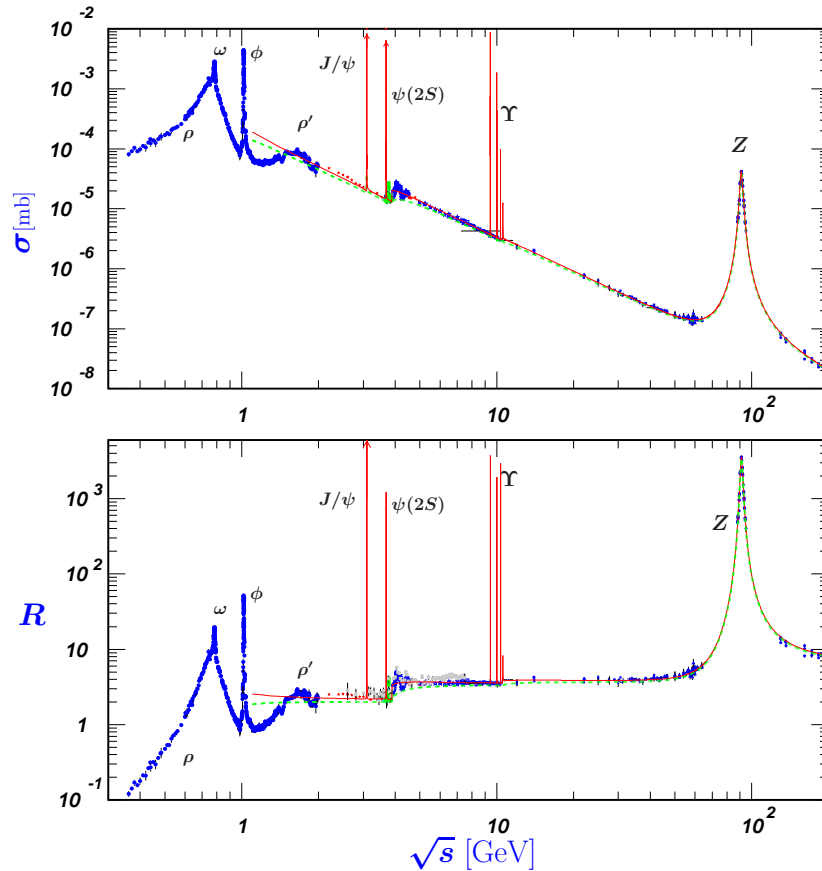
via low-energy theorem $\mathcal{L}_{\text{eff}} = \frac{H}{v} \left(G_{\mu\nu}^a \right)^2 \partial_{\ln m_t^2} \ln \frac{\alpha_s^{(5)}}{\alpha_s^{(4)}}$

[Chetyrkin et al. 1998]

(3) Quark masses at high precision

- central quantity in particle physics: the ratio $R(s) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$

- experiment:



- theory (naive):

parton model

$$R(s) \approx N_c \sum_q Q_q^2 \theta(\sqrt{s} - M_q)$$

$$\sim \left(\frac{4}{3} + \frac{1}{3} + \frac{1}{3} \right) + \frac{4}{3} + \frac{1}{3} + \frac{4}{3}$$

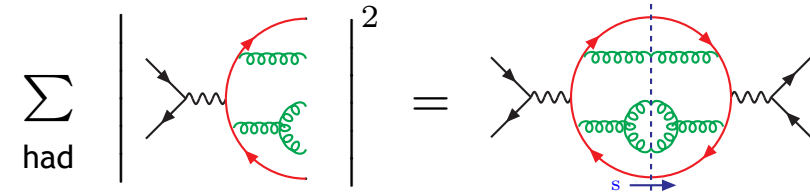
$u \quad d \quad s \quad c \quad b \quad t$

- ▷ rough structure OK
- ▷ details \rightarrow precision
- ▷ sharp resonances
e.g. J/ψ ($\bar{c}c$) or Υ ($\bar{b}b$)
- ▷ threshold behaviour

(3) Quark masses at high precision

- theory (precise):

unitarity connects $R(s)$ to correlator:



- ▷ resp. $R(s) \approx \Im \Pi(s - i\epsilon)$
- ▷ dispersion relation $\Pi(q^2) \sim q^2 \int ds \frac{R(s)}{s(s - q^2)} + \text{const}$

- strategy: $R^{exp} \stackrel{!}{=} R^{th}(\alpha_s, M_q)$

- ▷ determination of $\alpha_s \leftarrow$ consistent RG evolution $\leftarrow \beta(N_f = \text{light Quarks})$
+ decoupling of heavy Quarks (see above)
- ▷ determination of M_q

- main idea: Taylor coefficients of $\Pi \hat{=} \text{moments of } R(s)$

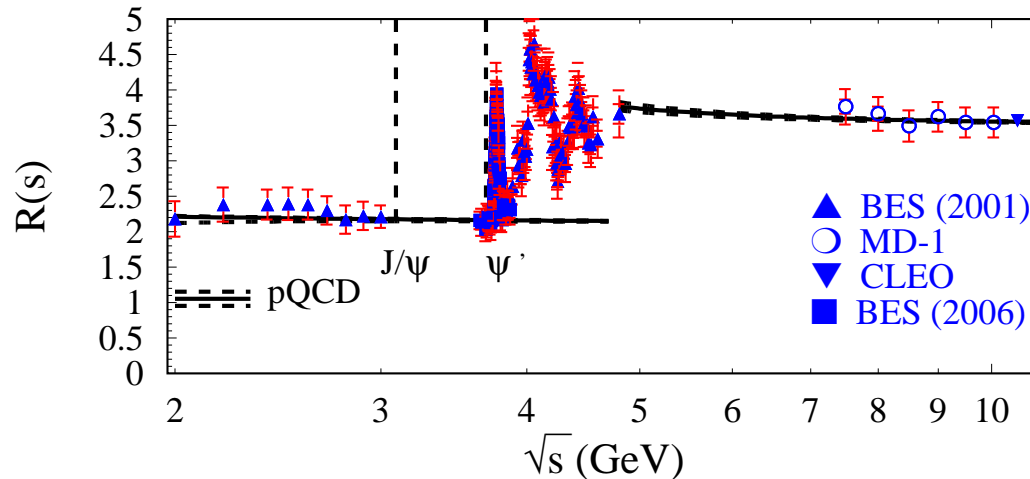
$$\mathcal{M}_n^{th} \sim \frac{1}{n!} \partial_{q^2}^n \Pi(q^2) \Big|_{q^2=0} \quad \text{vs} \quad \mathcal{M}_n^{exp} \sim \int \frac{ds}{s^{n+1}} R^{exp}(s)$$

th: expansion in q^2/M_q^2

- calculation: building blocks are vacuum tadpoles [YS, Vuorinen 2005; Boughezal, Czakon 2006]

(3) Quark masses at high precision

- experimentally determined moments: c -Quark threshold, $R(s)$ from 2 → 3.3



$$R^{exp} = R^{res} + R^{thr} + R^{cont}$$

- ▷ J/ψ : M 3 GeV, Γ 90 keV
- ▷ ψ : M 3.7 GeV, Γ 317 keV

$$\rightarrow \mathcal{M}_n^{exp}$$

- comparison: $\mathcal{M}_n^{th} \stackrel{!}{=} \mathcal{M}_n^{exp}$

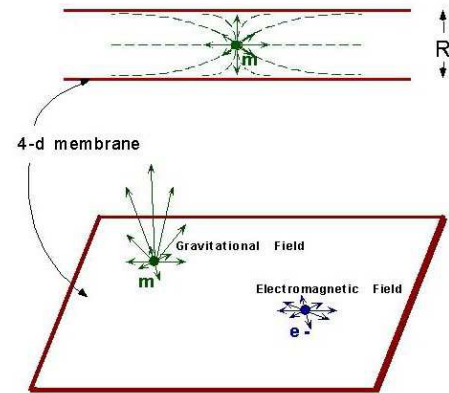
- ▷ $N_f = 4$ analysis $\rightarrow M_c(M_s) = 1.286(13)$ GeV [Kühn,Steinhauser,Sturm 2007]
- ▷ $N_f = 5$ analysis $\rightarrow M_b(M_b) = 4.164(25)$ GeV [dito]
- ▷ cf. PDG 2008: 1.27(11) and 4.20(17)

- why are precise Quark masses so important? e.g.

- ▷ B-Meson decays: $\Gamma(B \rightarrow X_u l \bar{\nu}) \sim G_F^2 M_b^5 |V_{ub}|^2$
- ▷ Υ spectroscopy: $M_{\Upsilon(1s)} = 2M_b(1 - \frac{2}{9}\alpha_s^2 + \dots)$
- ▷ Higgs-Boson decay (ILC): $\Gamma(H \rightarrow \bar{b}b) \sim G_F M_H M_b^2(1 + \alpha_s + \dots)$

What else could one dream to find?

E.g. extra (compact) dimensions



- main idea: explain feebleness of gravity by diluting it
 - ▷ gravitational fields allowed to fill more than 4 dimensions
 - ▷ ordinary matter and forces confined to (3+1) dim “3-brane”
 - ▷ \leftrightarrow motivation from string theory, 3+1+6 dim
 - ▷ e.g. ADD model: n compact extra dims, $M_F \sim \text{TeV}$: $M_P^2 \sim R^n M_F^{n+2}$
 - ▷ $\text{fm} \leq R \leq \text{mm}$ (gravity tests) $\Rightarrow 6 \geq n \geq 2$
- key collider signature: missing Energy! e.g. $q \bar{q} \rightarrow j G_{KK}(\cancel{E})$, $e^+ e^- \rightarrow \gamma G_{KK}(\cancel{E})$
 - ▷ Gravitons carry energy into extra dim
 - ▷ black hole production for $\sqrt{s} \gg M_F$
- many model variants: large-, universal-, warped-, ... -Xtra dim

Outlook

- have a **working** description of nature: Standard Model (SM)
 - ▷ will SM ‘‘survive’’ next decade?
 - ▷ many theoretical ideas for SM extensions
 - ▷ which ones are realized in nature?
- enormous experimental efforts
 - ▷ **LHC 2010+** → unprecedented energy range
- signals of ‘‘new’’ physics are extremely small
 - ▷ **highest precision** needed for background subtraction
- many opportunities for theory
 - ▷ contribute with moderate budget
 - ▷ key **building blocks**: SM parameters
 - ▷ scale dependence (evolution), mass effects
 - ▷ Bielefeld contributions: **QCD precision computations**
- this is truly the dawn of the LHC decade
 - ▷ discoveries could happen fast
 - ▷ fasten your seat belts!



LHC: Status 16 May 2010

LHC Page1

Fill: 1105

E: 1137 GeV

16-05-2010 19:17:43

BEAM SETUP: RAMP DOWN

Energy: 1137 GeV I(B1): 0.00e+00 I(B2): 1.61e+09

Post Mortem Information

PM event ID: Sun May 16 17:55:05 CEST 2010
 PM event category: PROTECTION_DUMP
 PM event classification: MULTIPLE_SYSTEM_DUMP
 PM BIS Analysis result: First input change detected: USER_PERMIT: Ch 13(TCDQ-b2): A T -> F on CIB.UA63..
 PM comment:

Comments 16-05-2010 18:08:52 :

	BIS status and SMP flags		B1	B2
Ramping Both beams lost! Later: one ramp at high intensity	Link Status of Beam Permits	false	false	false
	Global Beam Permit	false	false	false
	Setup Beam	true	true	true
	Beam Presence	false	false	false
	Moveable Devices Allowed In	false	false	false
	Stable Beams	false	false	false

LHC Operation in CCC : 77600, 70480

PM Status B1 **ENABLED** PM Status B2 **ENABLED**

QCD - Test (via large computer)

look at hadron spectrum (hadrons: bound states of quarks; e.g. $K=s\bar{d}$, $\rho=uud$, $\Lambda=uds$)

- solve QCD eqs by computer

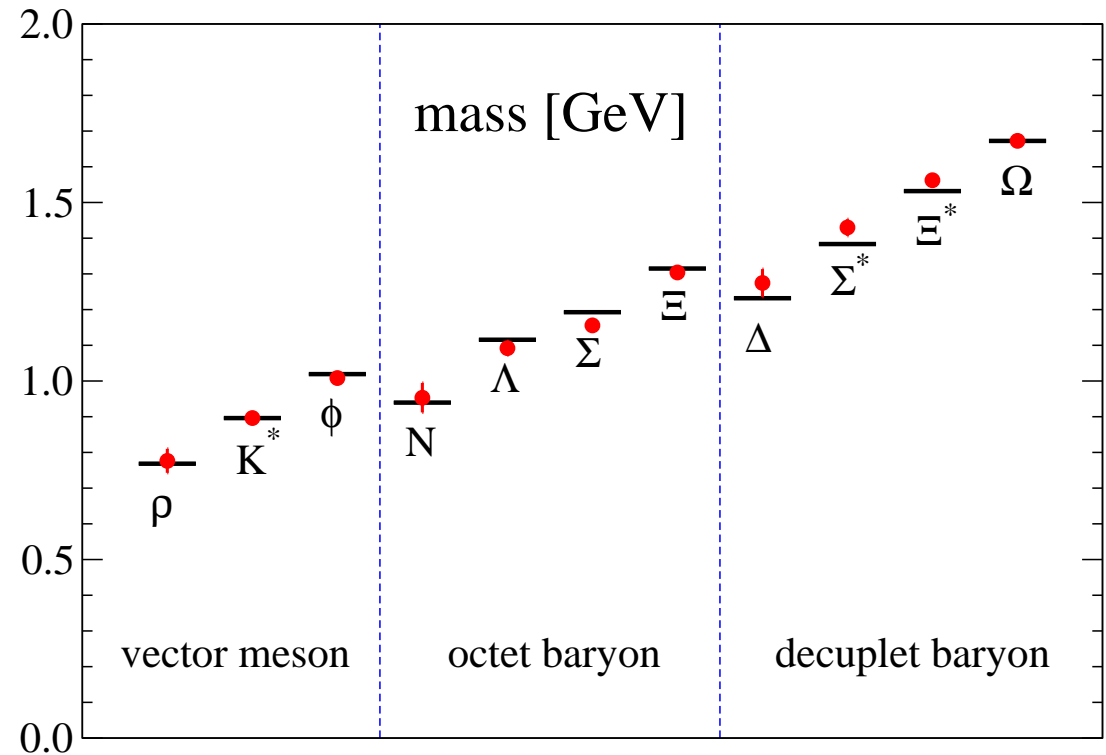
[e.g. S. Aoki et.al., PACS-CS 2008]

- what does not come out:

- ▷ gluons
- ▷ fractional charges

- what one gets:

- ▷ just the observed particles + masses
- ▷ no more, no less!



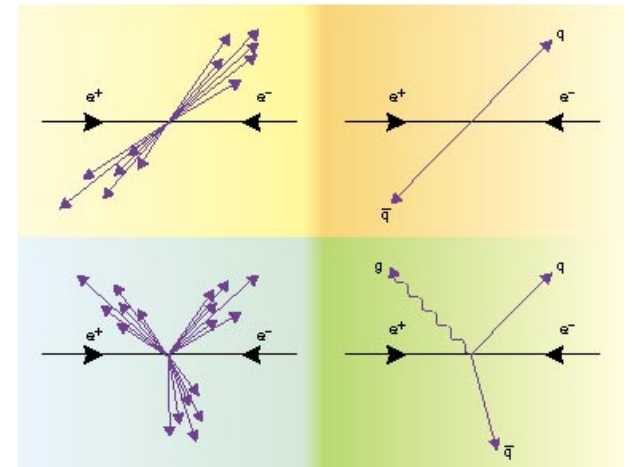
- punchline: QCD postdicts the low-lying hadron masses!

- ▷ much development here; teraflop speeds, worldwide effort
- ▷ $a = 0.091$ fm; $32^3 \times 64$ lattice; NP $\mathcal{O}(a)$ impr. Wilson quarks
- ▷ 2+1 flavors; chiral logs; $m_q \approx 1.3 m_l$; π , K , Ω as input

SM-Test (with colliders)

- e.g. LEP, $e^+e^- \rightarrow X$ (stuff hitting detector): find 2 broad classes of events (QM!)
- (1) $X = e^+e^-$ or $\tau^+\tau^-$ or ... l^+l^-
 - ▷ leptons: no color charge \rightarrow mainly QED interactions
 - ▷ simple final state: coupling small ($\alpha = e^2/(4\pi) \approx 1/137$)
most of the time (99%) nothing happens
 - ▷ $e^+e^- \gamma \sim 1\% \rightarrow$ check details of QED
 - ▷ $e^+e^- \gamma\gamma \sim 0.01\% \rightarrow \dots$

- (2) $X > 10$ particles: $\pi, \rho, p, \bar{p}, \dots$
 - ▷ “greek+latin soup” constructed from qu+gl
 - ▷ pattern: flow of E+momentum in “jets”
 - ▷ 2 jets $\sim 90\%$; 3 jets $\sim 9\%$; 4 jets $\sim 0.9\%$
 - ▷ direct confirmation of asy. freedom!
 - ▷ hard radiation is rare \rightarrow # of jets
 - ▷ soft radiation is common \rightarrow broadens jet



- nowadays: “testing QCD” \rightarrow “calculating backgrounds” in search for new phenomena
discrepancies \rightarrow “new” physics

Concepts and Methods

techniques used

- computer algebra
 - ▷ generation of Feynman diagrams
 - ▷ classification; scalarization
 - ▷ reduction to ‘‘master integrals’’
- evaluation of master integrals
 - ▷ numerical integration: precision ?
 - ▷ explicit integration: ‘‘art’’
 - ▷ difference equations: analytical/numerical solution
 - ▷ differential equations
- effective field theory → integrate out heavy Quarks

[J. Möller (PhD student)]

[E. Bejdakic (PhD student)]

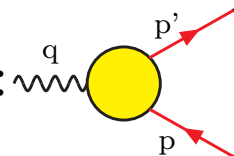
tools

- FORM + computer cluster
- special functions
 - ▷ harmonic polylogarithms $HPL(x)$ [Remiddi, Vermaseren 2000]
 - ▷ multiple harmonic sums $S(N)$ [Vermaseren 1998]
- new/innovative/combined tools?! large N? AdS/CFT? Hopf algebra?

Lepton magnetic moments

- prediction of Dirac theory: $\mu_l = 2 \frac{e\hbar}{2m_l} s \quad (l \in \{e, \mu, \tau\})$

- quantum corrections: $2 \rightarrow 2(1 + a_l)$

- computation:  $= \bar{u}(p') \left[\gamma^\mu F_1(q^2) + i \frac{\sigma^{\mu\nu} q_\nu}{2m_l} F_2(q^2) \right] u(p)$

- relationship: $a_l = F_2(0)$

▷ experiment: $a_\mu = 116592080(63) \cdot 10^{-11}$

▷ theory: $a_\mu^{QED} = \frac{1}{2\pi}\alpha + \dots + \# \alpha^4 + ?? \alpha^5$

where $\alpha \approx 1/137$

α^1 : [Schwinger 1948]

[N.Groeger, T.Luthe, J.Schücker (BA students)]

$\alpha^4 \approx 380 \cdot 10^{-11}$ [Kinoshita et al. 2002; Laporta, Remiddi 2006]

α^5 : [Kinoshita et al., in progress]

▷ theory: a_μ^{EW} incl 2-loop OK

- comparison: “interesting discrepancy” of 3σ
(1.8σ with τ -data for hadronic effects)